

# RESIDUAL STRESSES IN RAILS

**Si Hai Mai, M.-L. Nguyen-Tajan**

SF2M, 13<sup>th</sup> March 2014

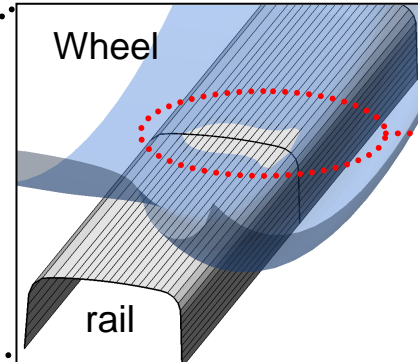
**SNCF - Innovation & Research, Paris**



# Context



**Loading cycles** on the rail = a lot of trains circulations



**Wheel-rail contact**  
(Rolling contact)

High pressure on a small contact area

Ex: High Speed Train (TGV) = 12Tones/1cm<sup>2</sup>

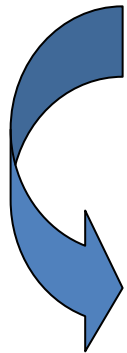


**Fatigue crack** in the rail

*Rail rolling contact fatigue is the cause of (From SNCF):*

- ~ 50% of rail fractures (taking account weld's fracture)
- ~ 70% of the number of rail replacements

# Context

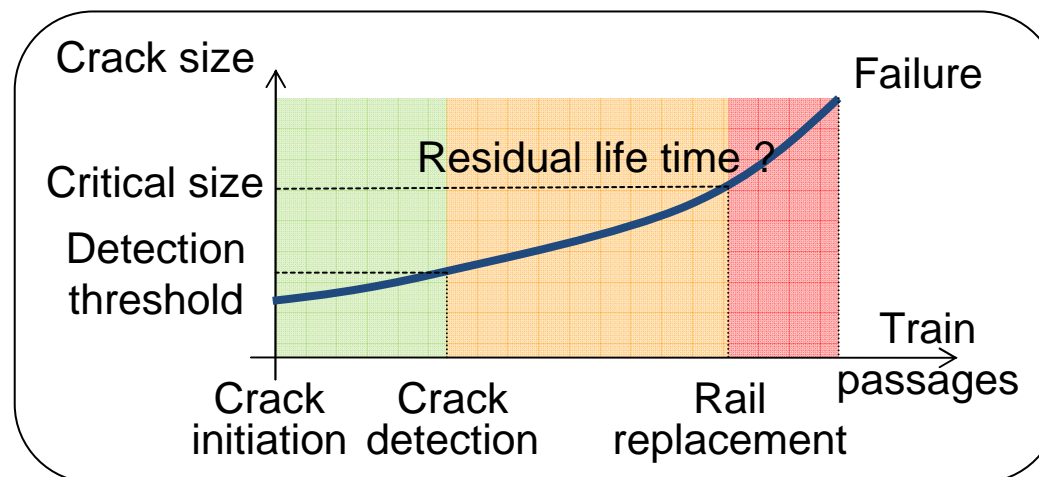


## Rail contact fatigue cracks

- Costly maintenance operations, train delays
- **Safety** issues (Ex: derailment causing by rail fracture)

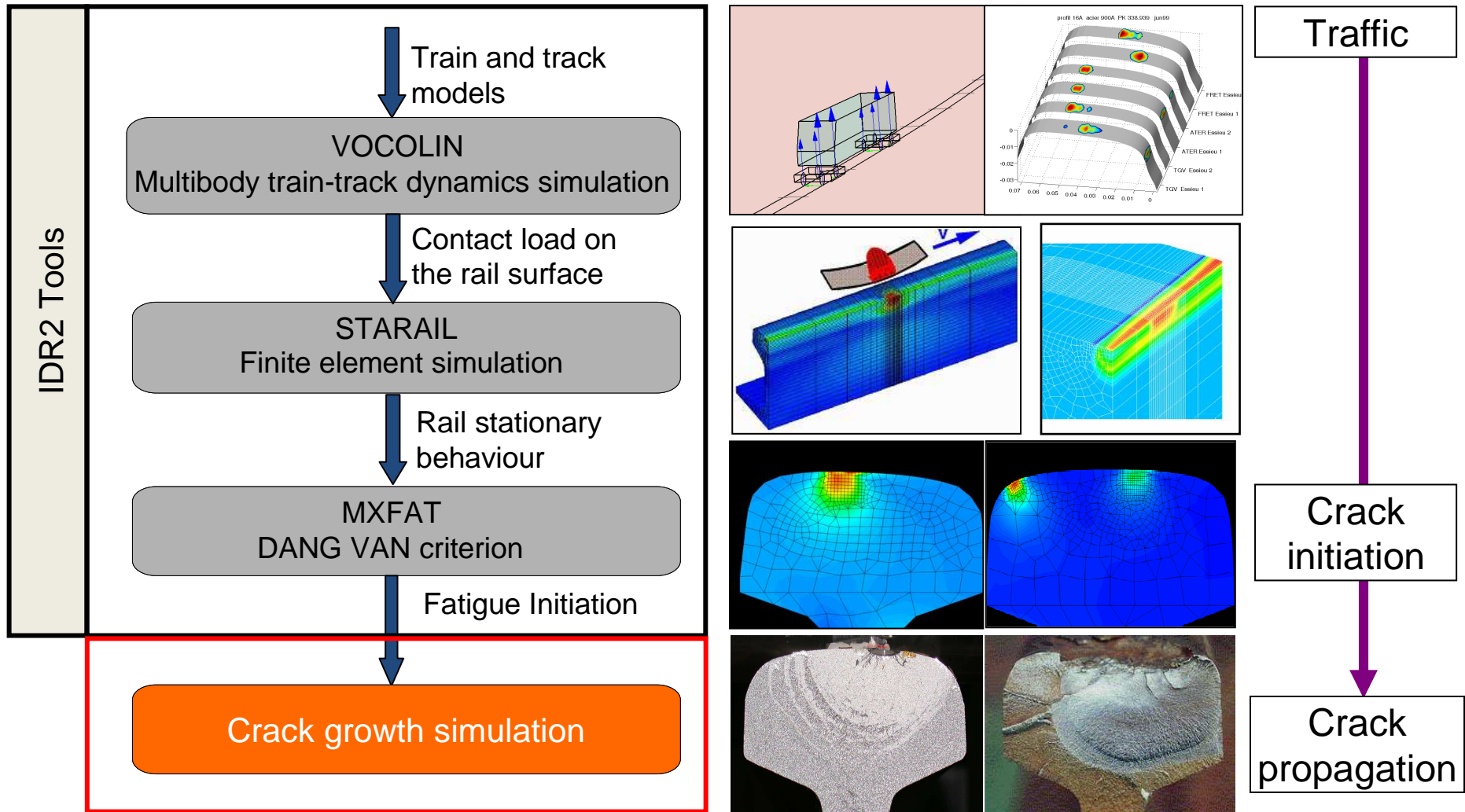
## Objectives

- Improve the understanding of the rail fatigue damage behavior
- Develop numerical tools for prediction of crack growth in the rail
- Optimize the maintenance strategy (grinding, inspection planning)



# Context

## From a dynamics simulation to the crack propagation



IDR2 = Initiative for **D**evelopment **R**esearch on **R**ail

# Outline

I. Context

## II. Residual stresses in Rails

III. Fatigue crack growth simulations

IV. Conclusions

# Sources of residual stresses in the rail

## Two sources:

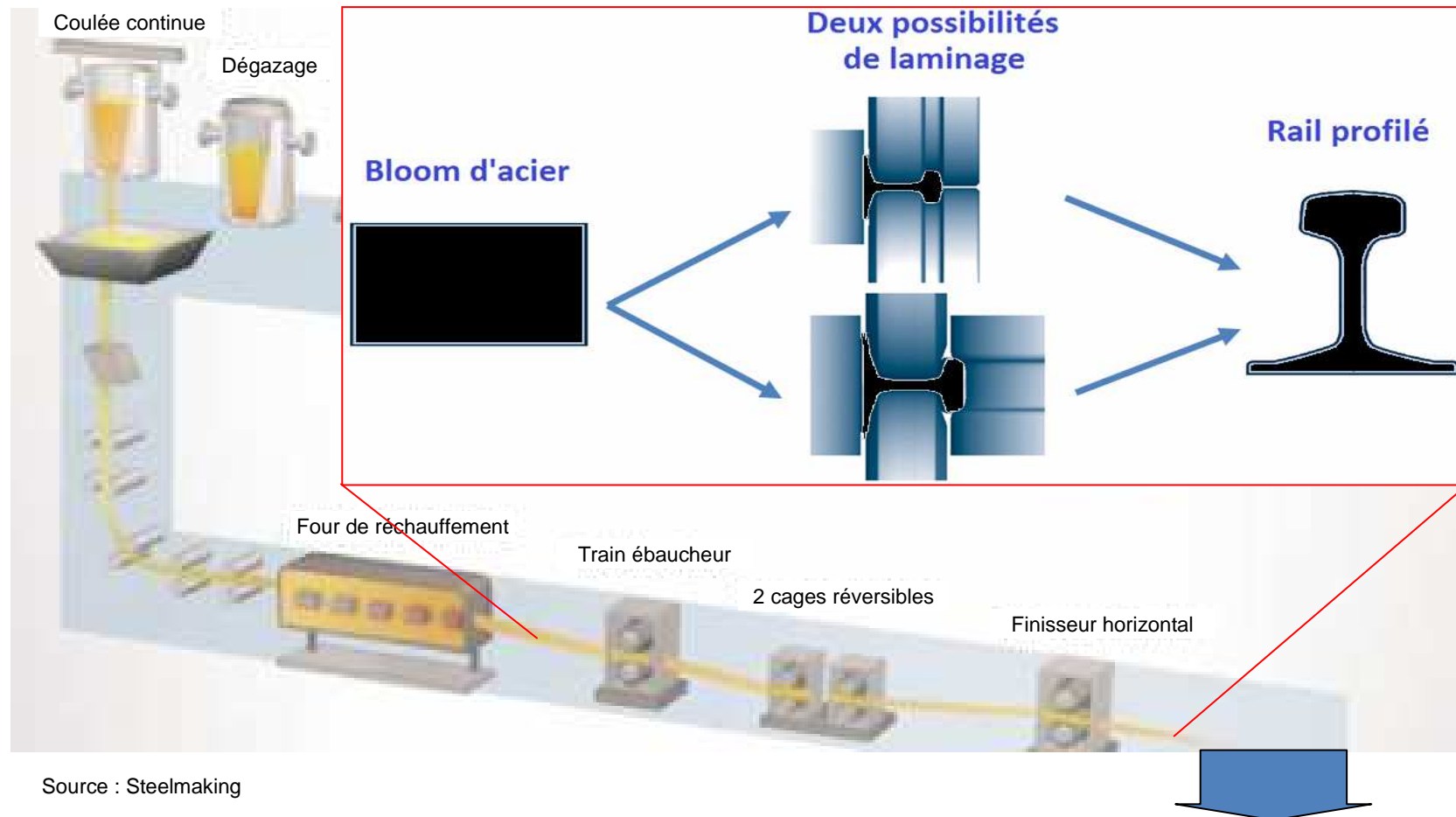
- **Roller straightening** = Manufacturing process
- **Train passages** = Plastic strain accumulation due to the repeated load



Thermal stresses (Summer – Winter) = Increase or decrease the risk of final Fracture

# Sources of residual stresses in the rail

## Manufacturing process



# Sources of residual stresses in the rail

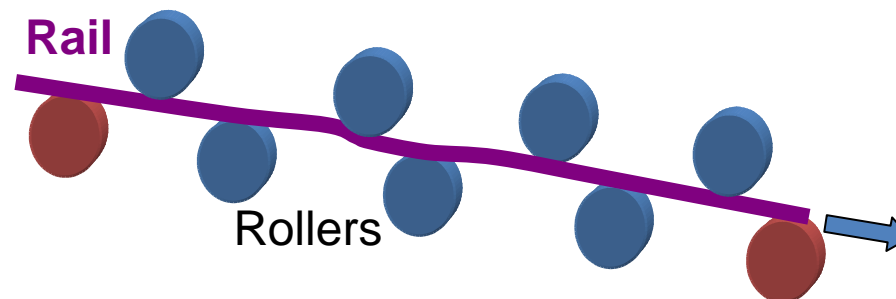
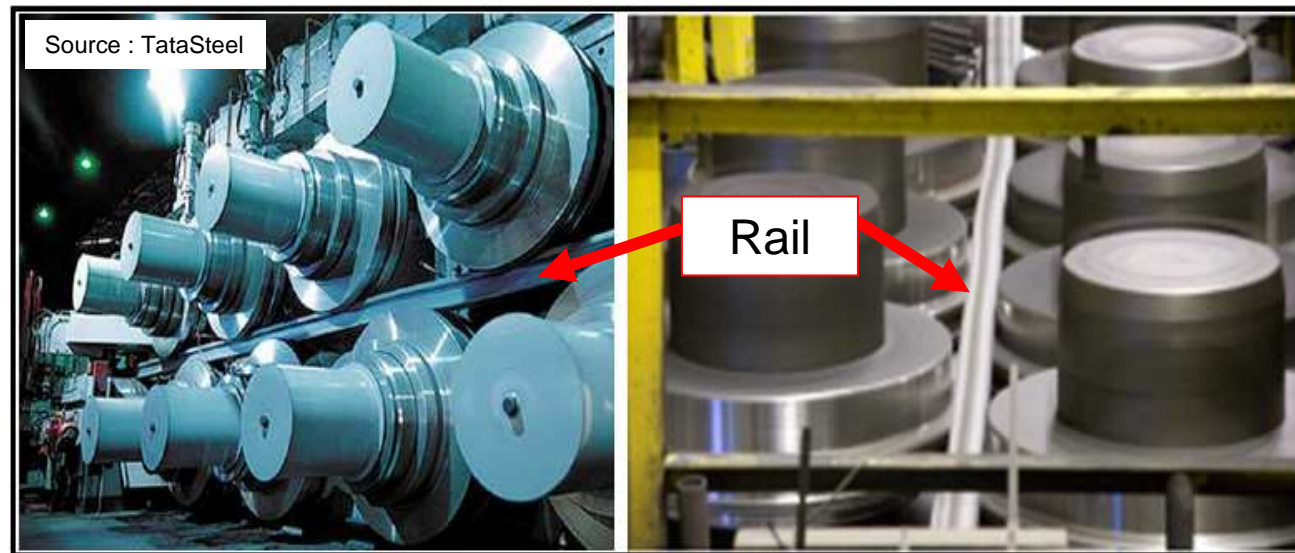
## Manufacturing process





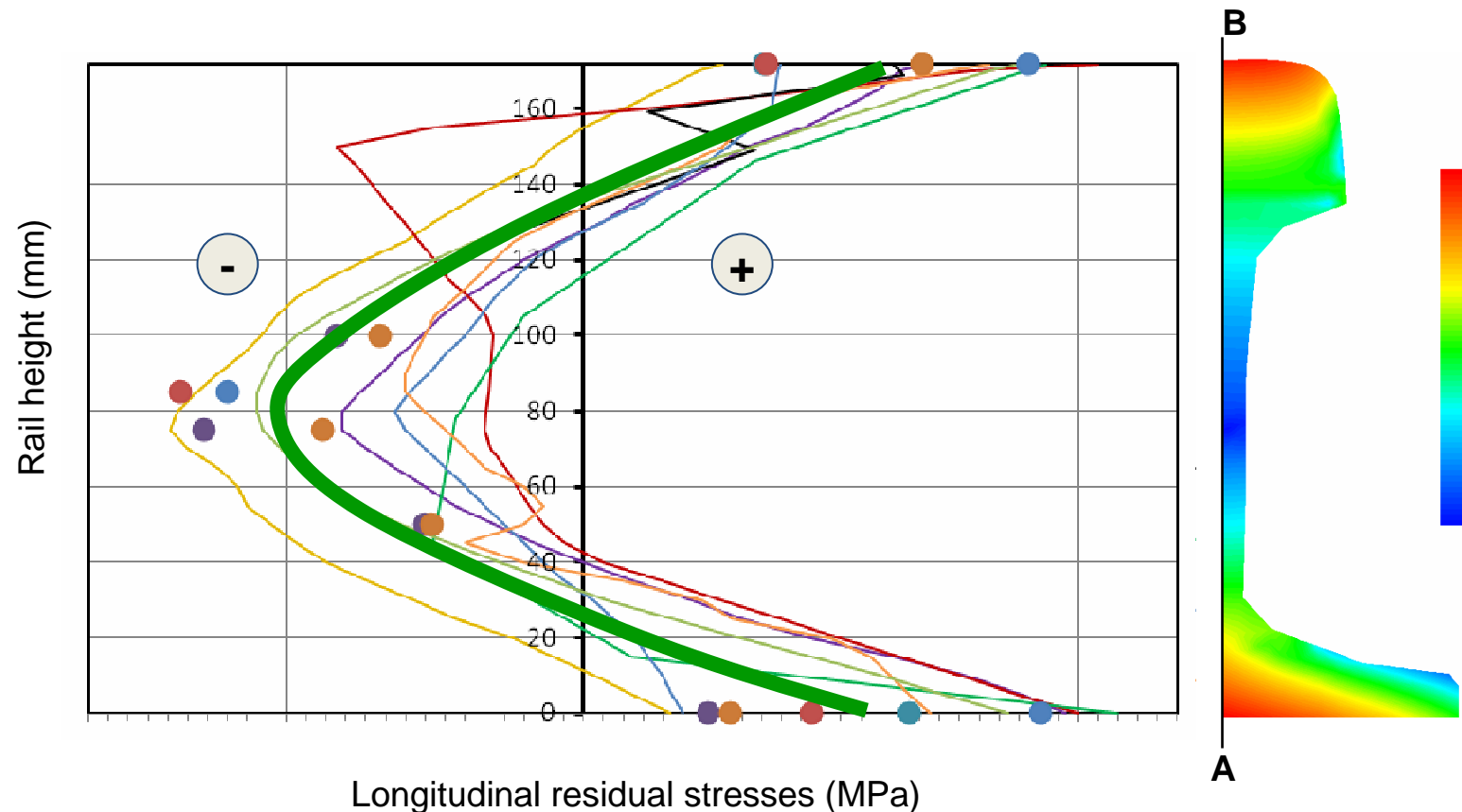
# Sources of residual stresses in the rail

## Manufacturing process (Roller straightening)



# Sources of residual stresses in the rail

## Manufacturing process (Roller straightening)

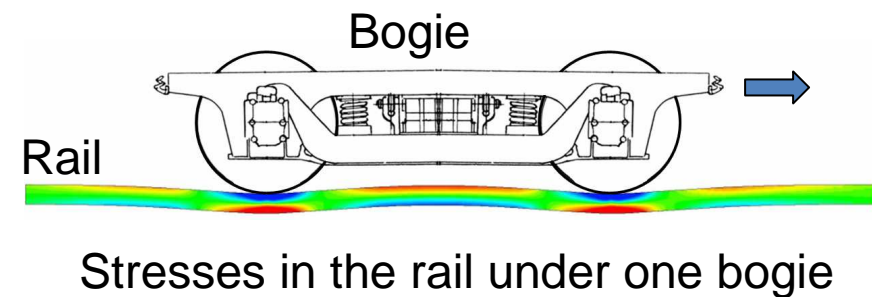
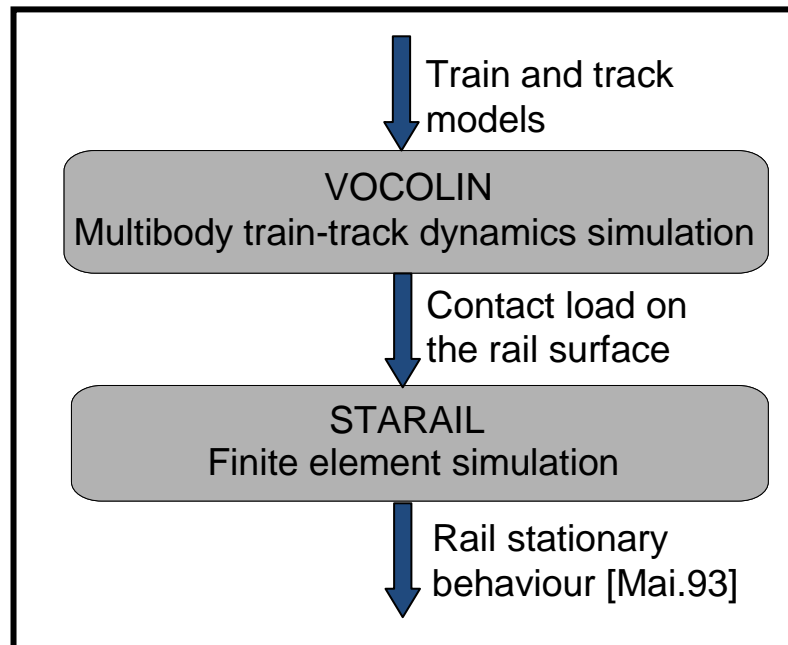


Without thermal treatment

# Sources of residual stresses in the rail

## Train passages

➔ Plastic strain accumulation due to the repeated load

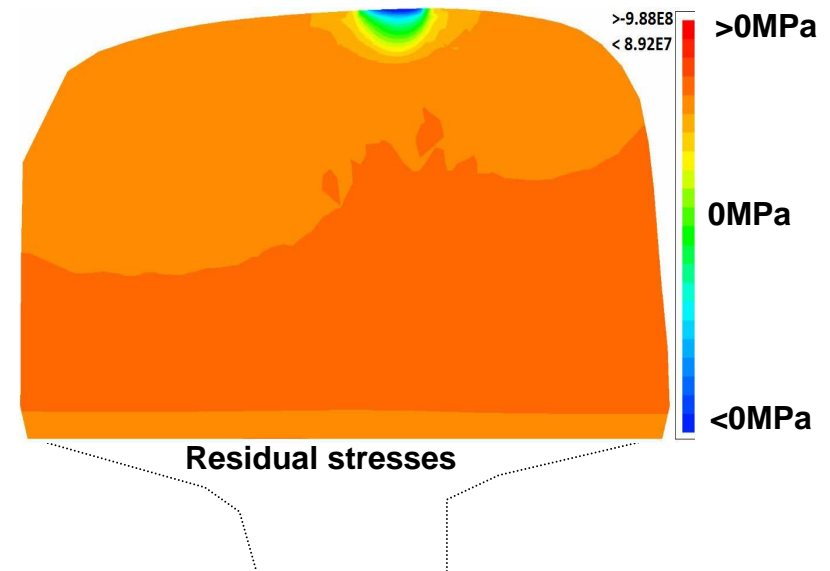
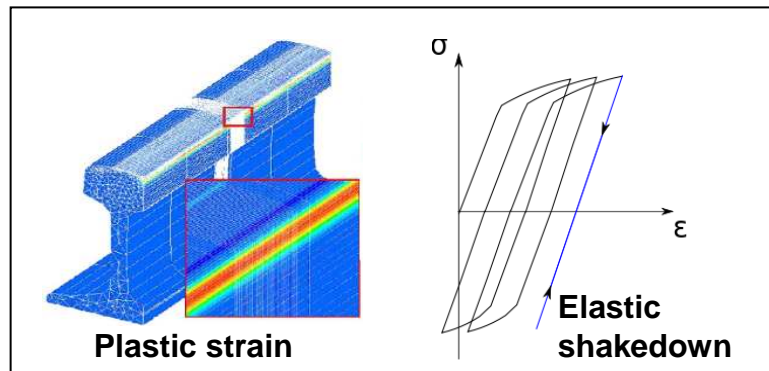


*H. Maitournam and K. DangVan 1993: J. Mech. Phys. Solids, 41 (1993) 1691-1710*

# Sources of residual stresses in the rail

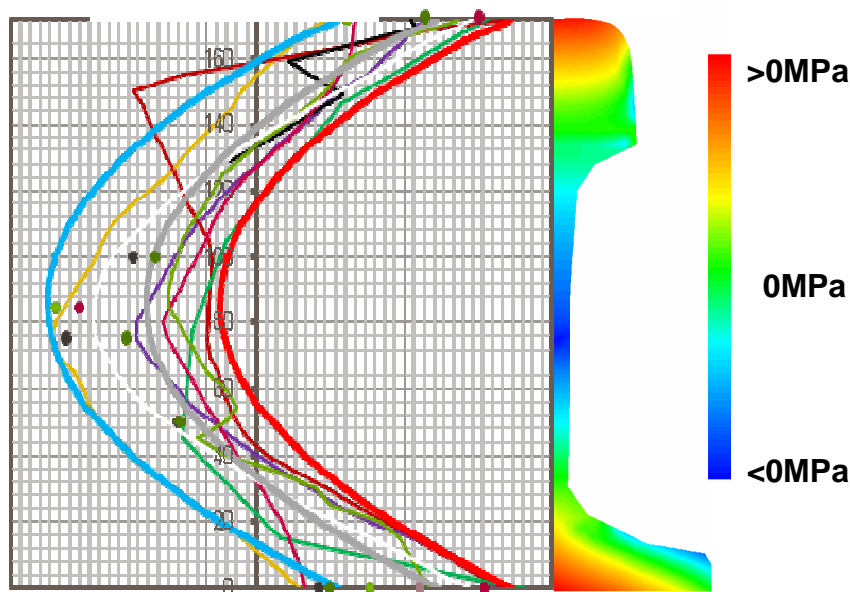
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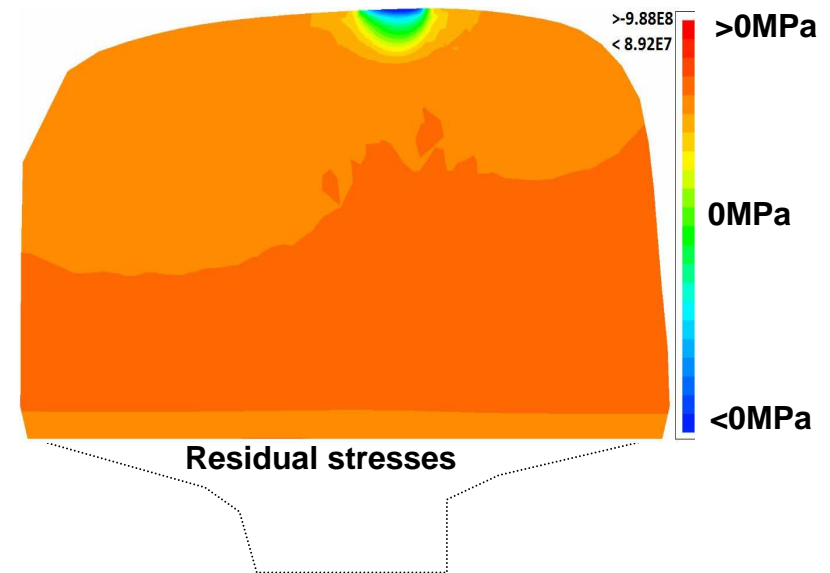


# Sources of residual stresses in the rail

## Two sources:



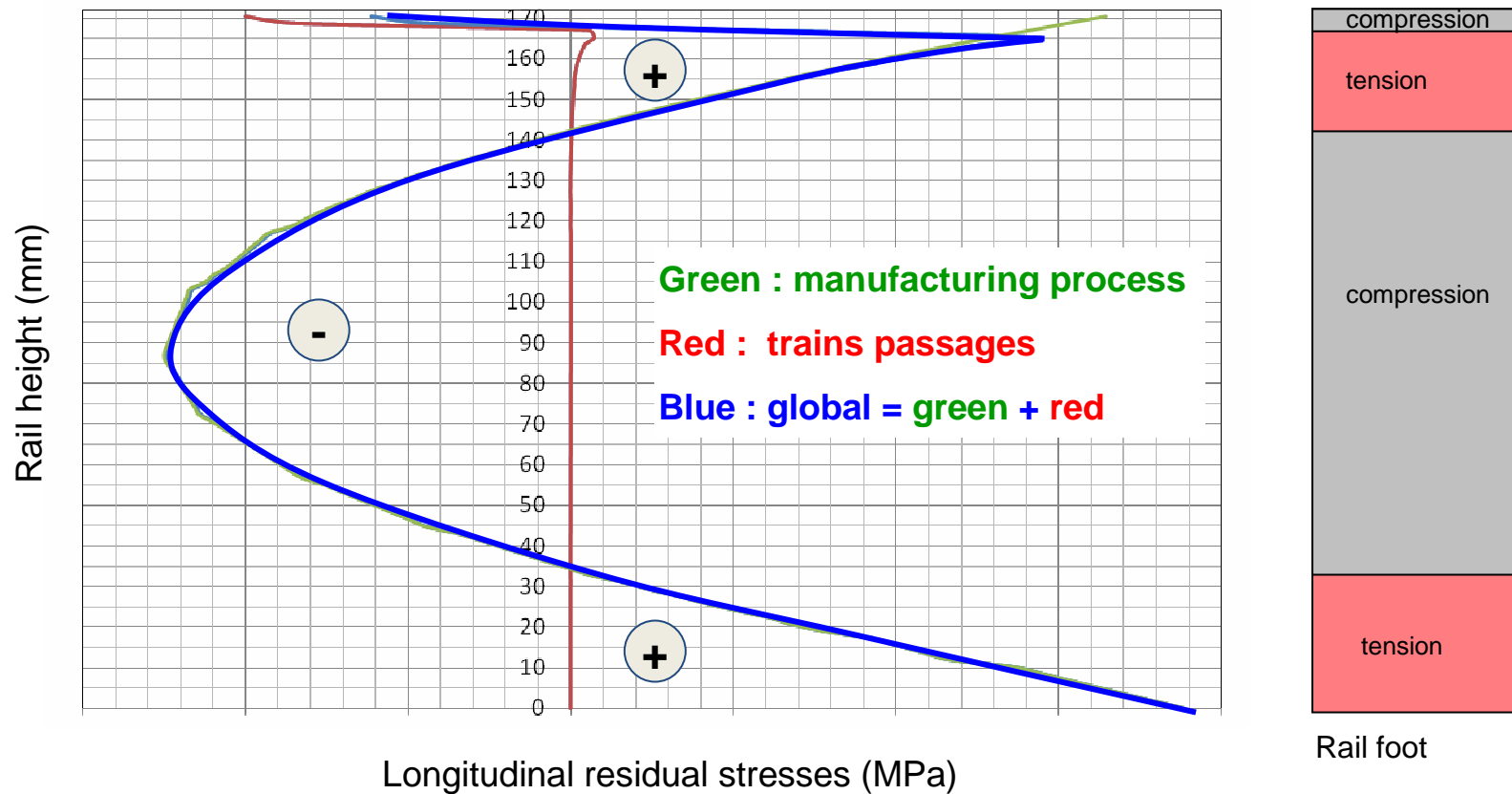
Manufacturing process



Train passages

# Sources of residual stresses in the rail

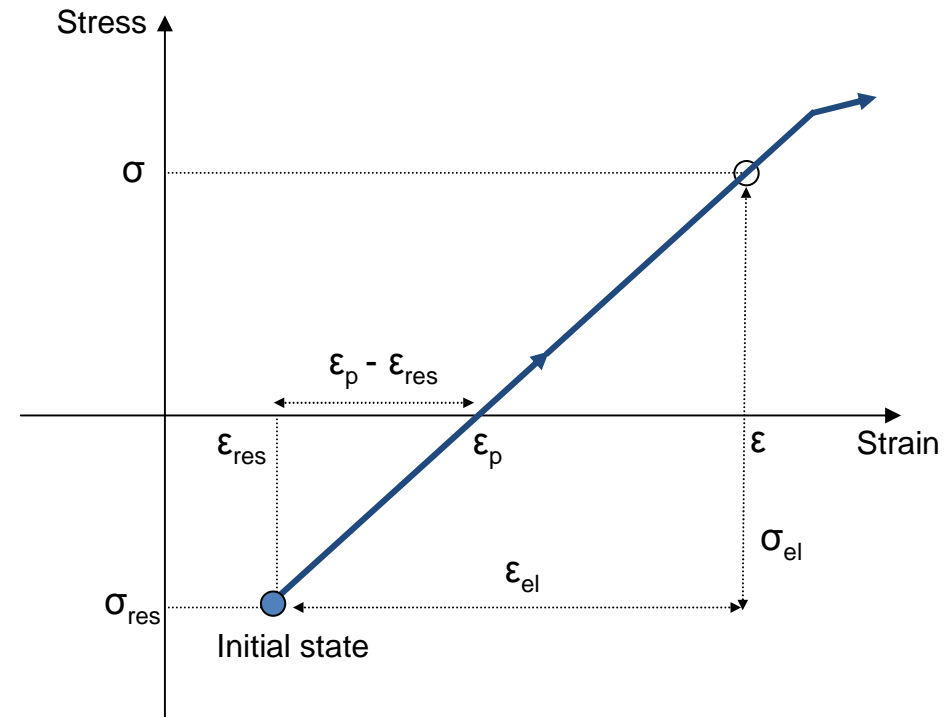
## Two sources:



# Procedure of integration of residual stresses

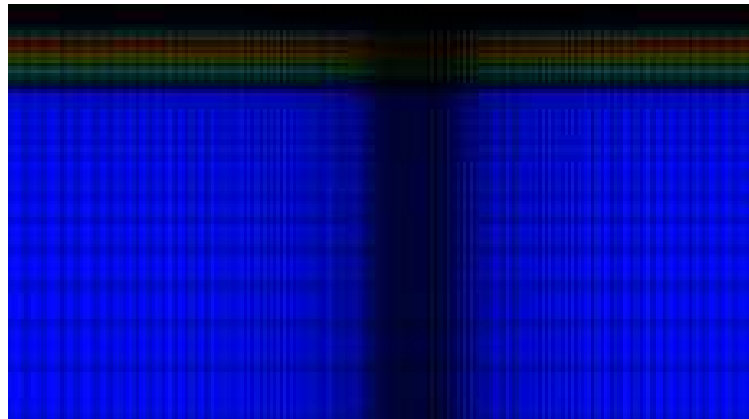
$$\begin{cases} \underline{\xi} = \underline{\xi}_{res} + \underline{\xi}_{el} \\ \underline{\varepsilon} = \underline{\varepsilon}_{res} + \underline{\varepsilon}_{el} \\ \underline{\sigma} = \underline{\sigma}_{res} + \underline{\sigma}_{el} \end{cases}$$

$$\begin{cases} \underline{\xi} = \left[ \underline{\underline{K}}^{-1} \right] \cdot \left[ -\text{div}(\underline{\underline{C}} : \underline{\varepsilon}_p) + \underline{F}_{el} \right] \\ \underline{\varepsilon} = \frac{1}{2} (\underline{\nabla} \underline{\xi}_{res} + {}^T \underline{\nabla} \underline{\xi}_{res}) + \frac{1}{2} (\underline{\nabla} \underline{\xi}_{el} + {}^T \underline{\nabla} \underline{\xi}_{el}) \\ \underline{\sigma} = \underline{\underline{C}} : (\underline{\varepsilon}_{el} + \underline{\varepsilon}_{res} - \underline{\varepsilon}_p) \end{cases}$$



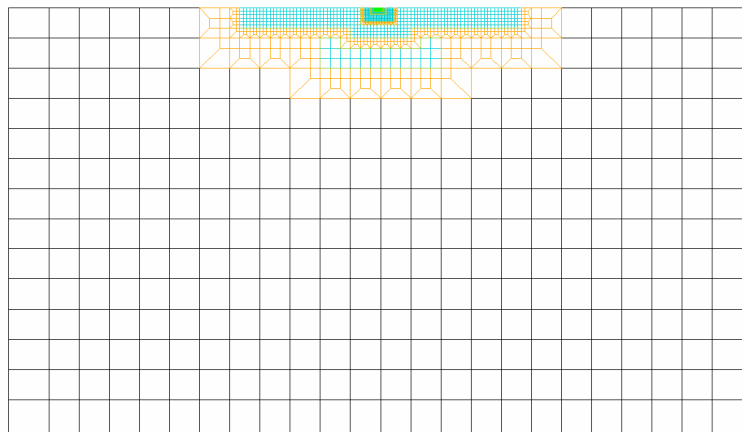
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# Procedure of integration of residual stresses



Stationary calculation (FEM)

Different meshes  
↓  
**Projection**



Crack propagation (XFEM)



# Outline

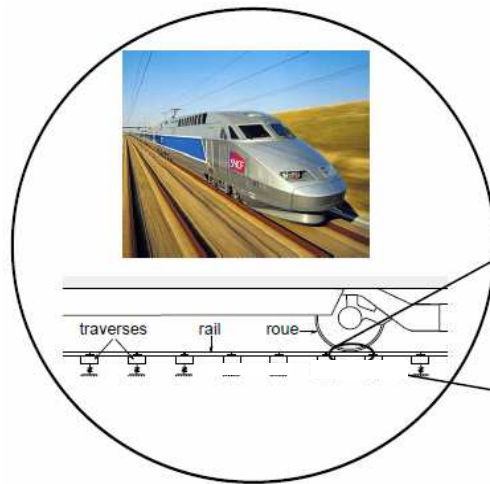
I. Context

II. Residual stresses in rails

**III. Fatigue crack growth simulations**

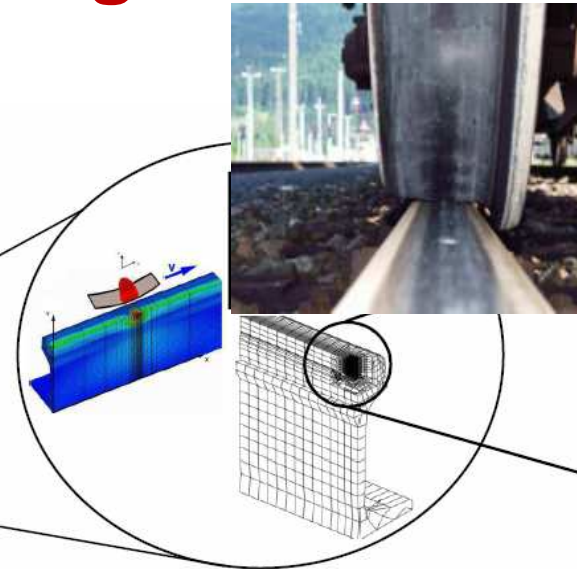
IV. Conclusions

# Rolling contact fatigue : a multi-scale problem



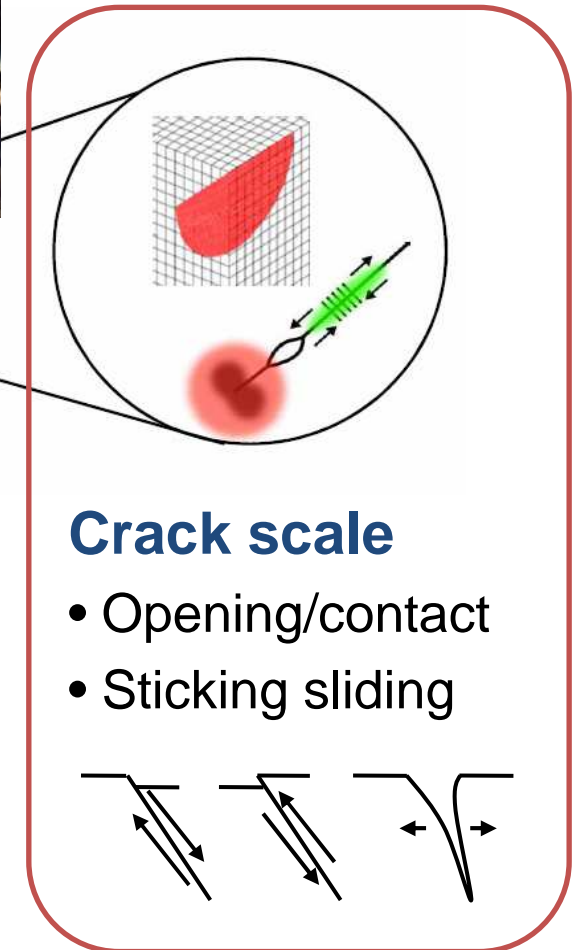
## System scale

- Rail bending



## Rail scale

- Wheel rail contact

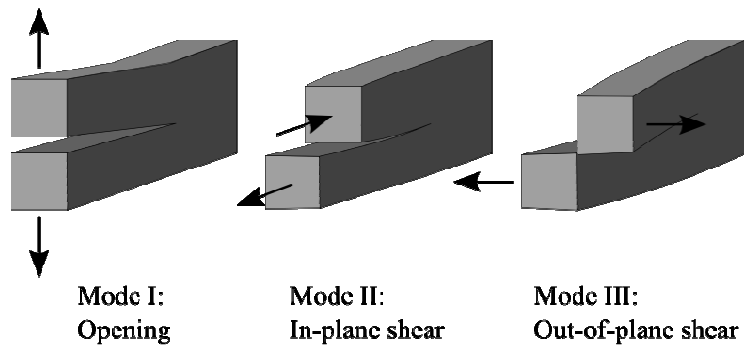


## Crack scale

- Opening/contact
- Sticking sliding

# Methodology

## Linear Elastic Fracture Mechanics



## Stress singularity at the crack front

$$\sigma_{ij} = \frac{K_I}{\sqrt{2\pi r}} f_{ij}^I(\theta) + \frac{K_{II}}{\sqrt{2\pi r}} f_{ij}^{II}(\theta) + \frac{K_{III}}{\sqrt{2\pi r}} f_{ij}^{III}(\theta) + o(\sqrt{r})$$

$K_i$  characterizes the solicitations at the crack tip  
(= Magnitude of each cracking mode)

**CAST3M**

*Gravouil, Combescure, Pommier and Moës 2011 : XFEM for crack propagation*

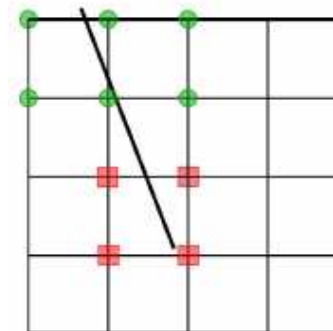
## The eXtended Finite Element Method (X-FEM) [Gra.11]

- Two scale approach :

$$U = U_{\text{bulk}} + U_{\text{crack}}$$

- Two kinds of enrichment :

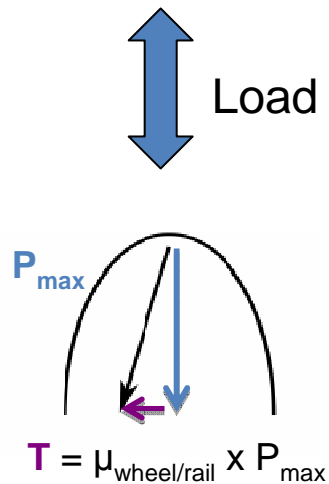
- Discontinuous (lips displacement)
- Singular (crack tip)



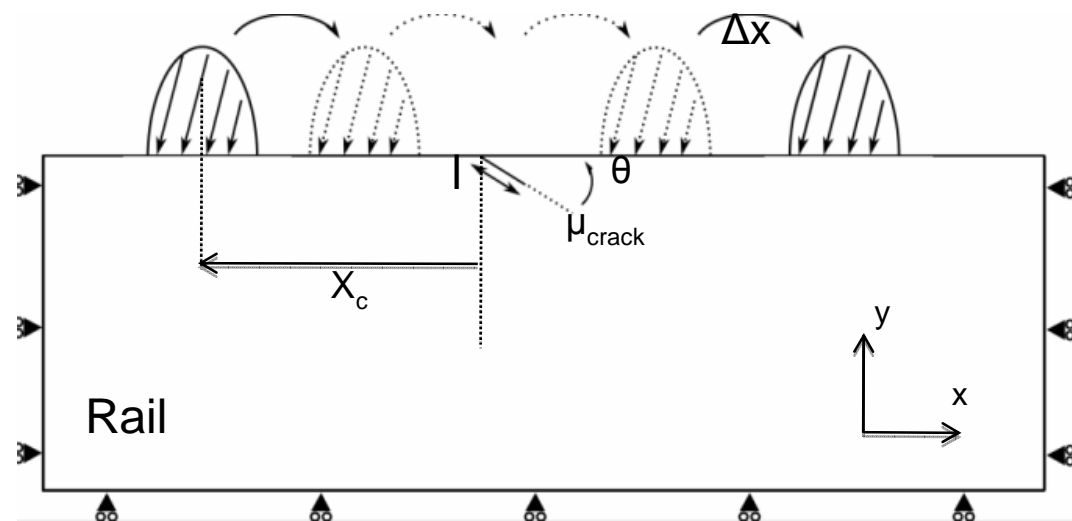
# Modelling of the cracked rail



1 loading cycle = 1 wheel traveling from the left to the right on the surface of the rail (quasi-static simulation)

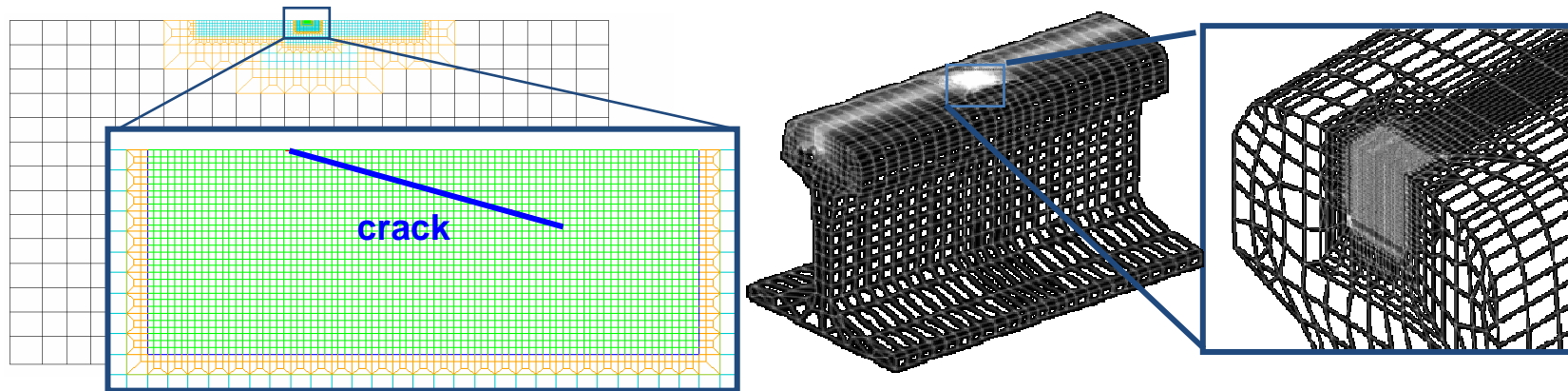


**HERTZIAN LOADING**



# Modelling of the cracked rail

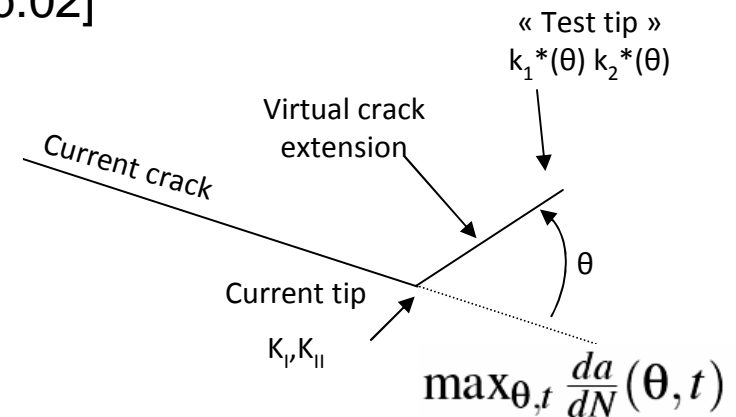
- Multi-scale parametric mesh (software CAST3M)



- Crack growth rate law: Mixed mode (ICON) [Dub.02]

$$\frac{da}{dN} = 2.10^{-9} (\Delta K_{eq})^{3.33} \quad \Delta K_{eq}^2 = \Delta K_I^2 + 0.772 * \Delta K_{II}^2$$

- Crack branching criterion: Multi-axial and non proportional loading [Hou.82]

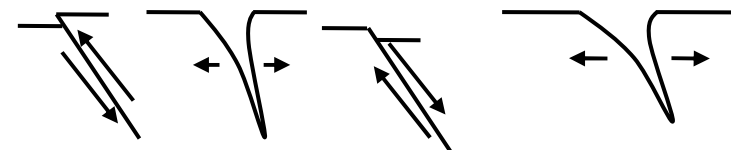
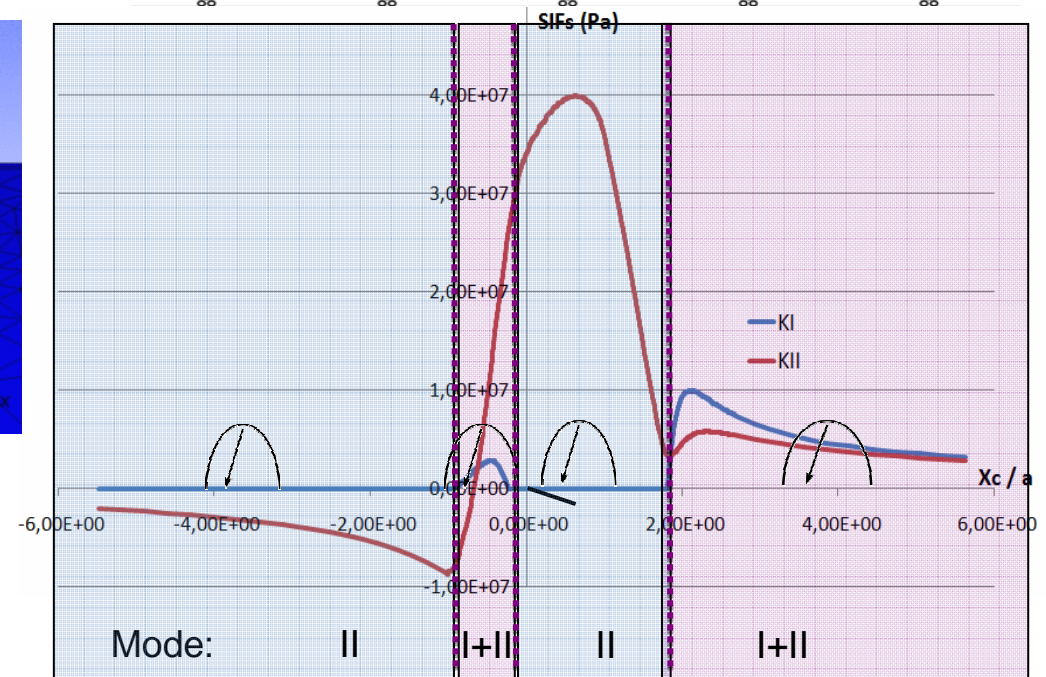
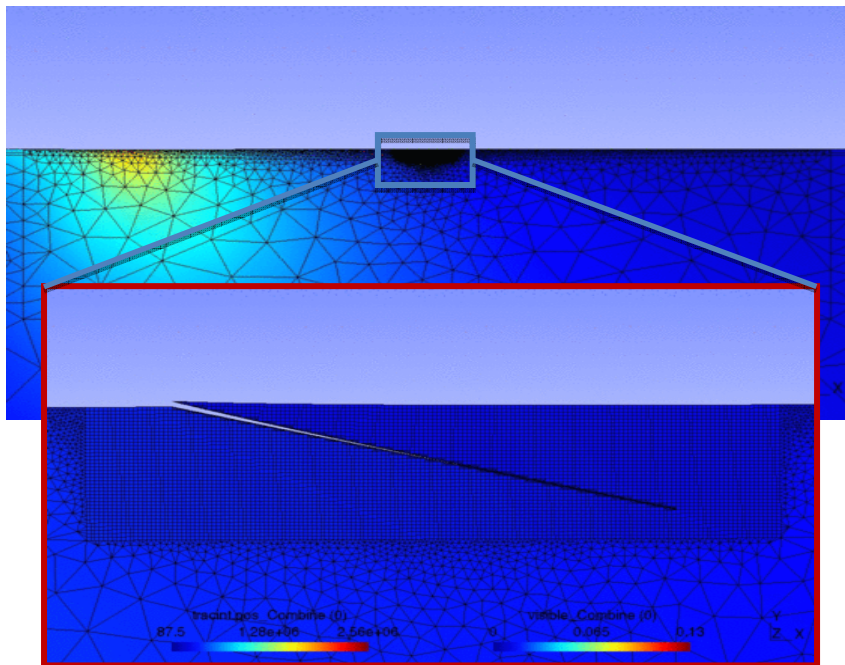
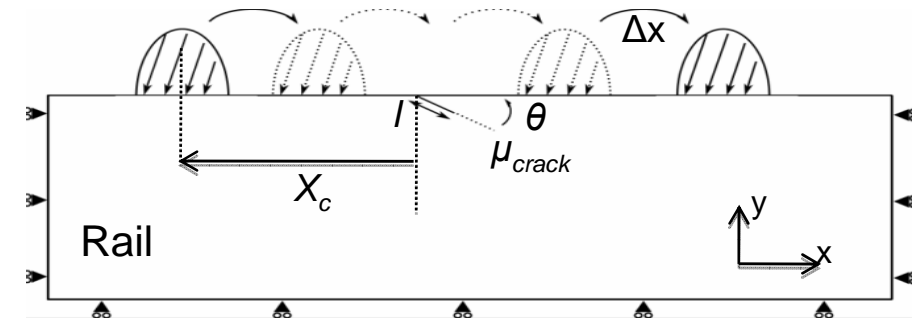


*Dubourg 2002: Journal of Tribology, Vol. 124.*

*Hourlier nad al. 1982 : Institut de Recherche de la sid rurgie fran aise, IRSID, No RE958*

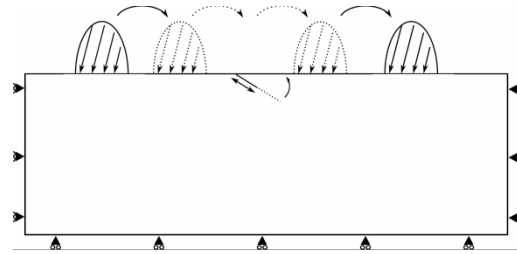
# Calculation of SIF for one loading cycle : 2D

Stress Intensity Factors (SIF) are computed for each time step (each loading position)

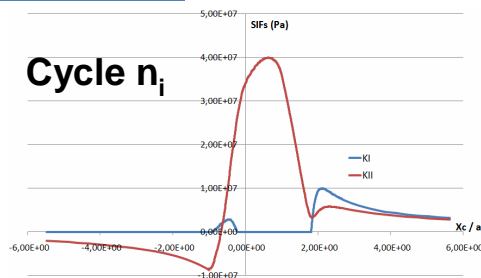




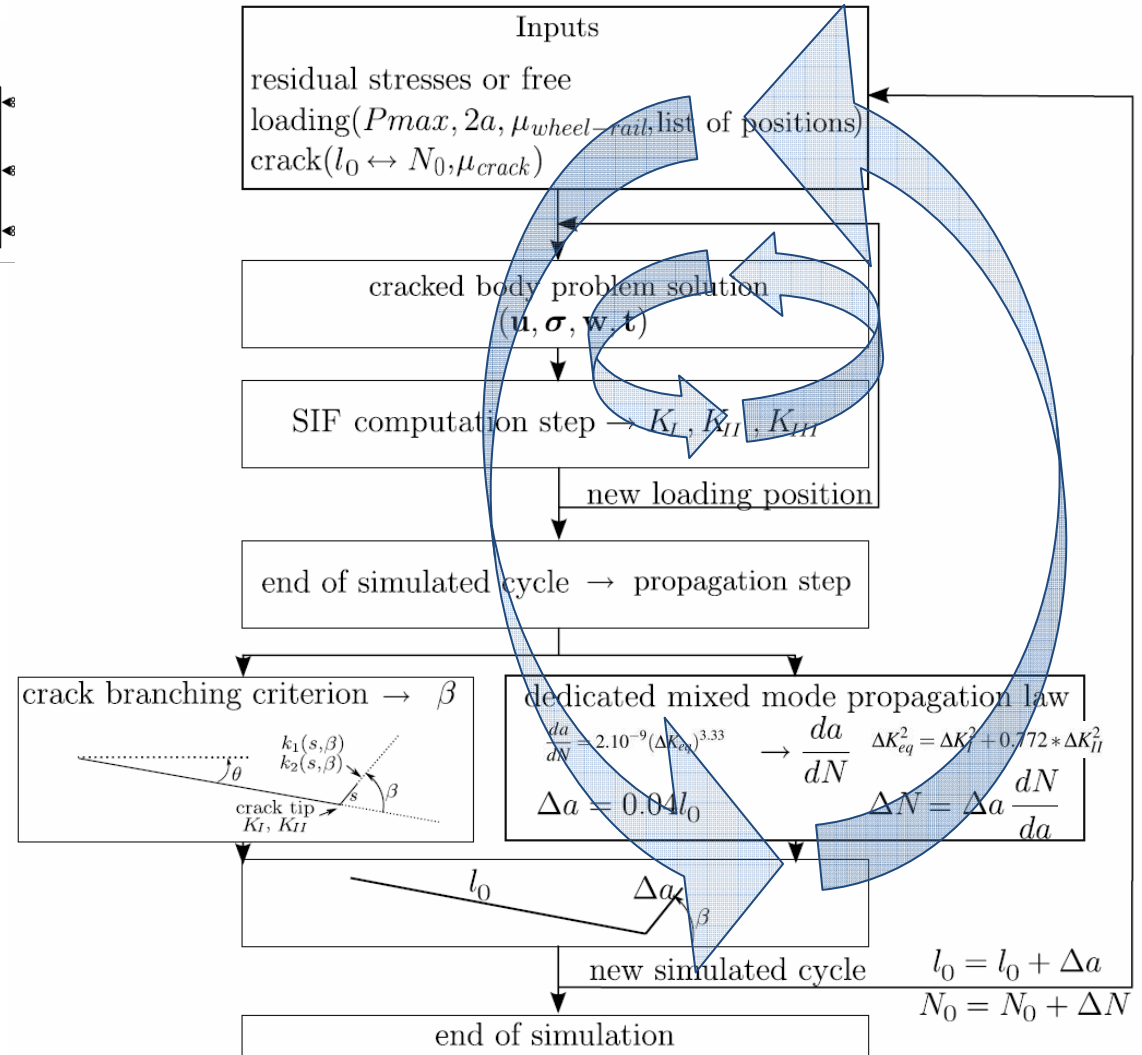
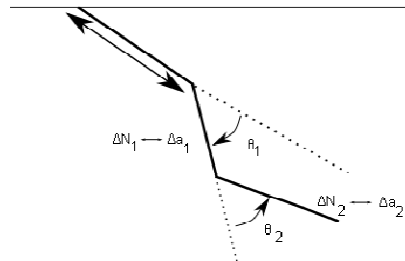
# Fatigue crack growth simulation process



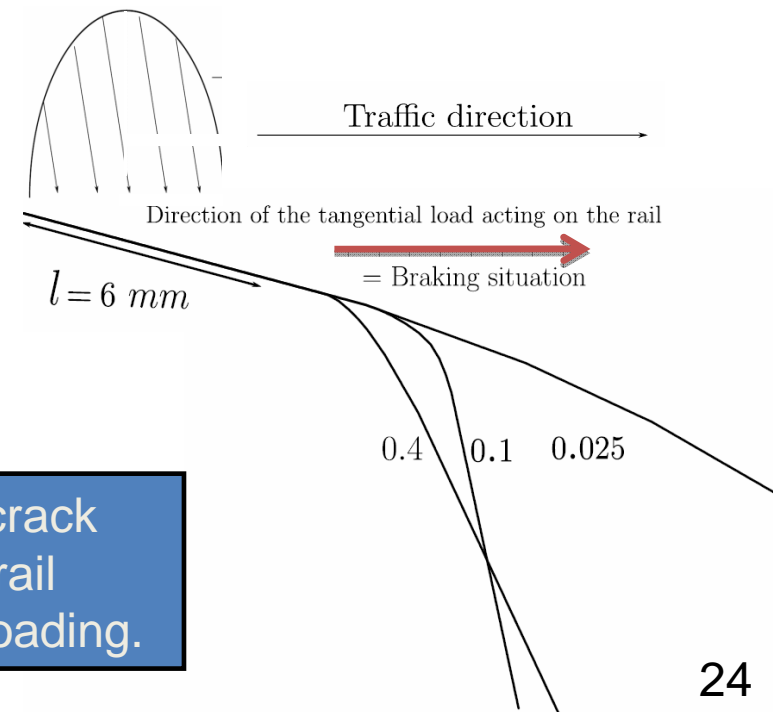
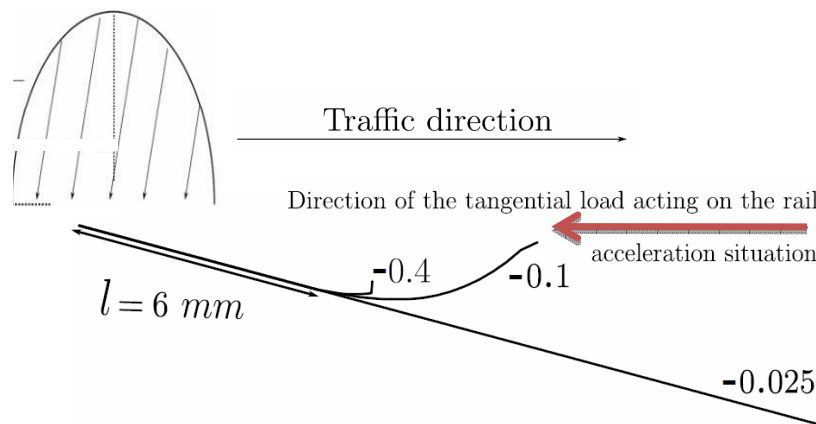
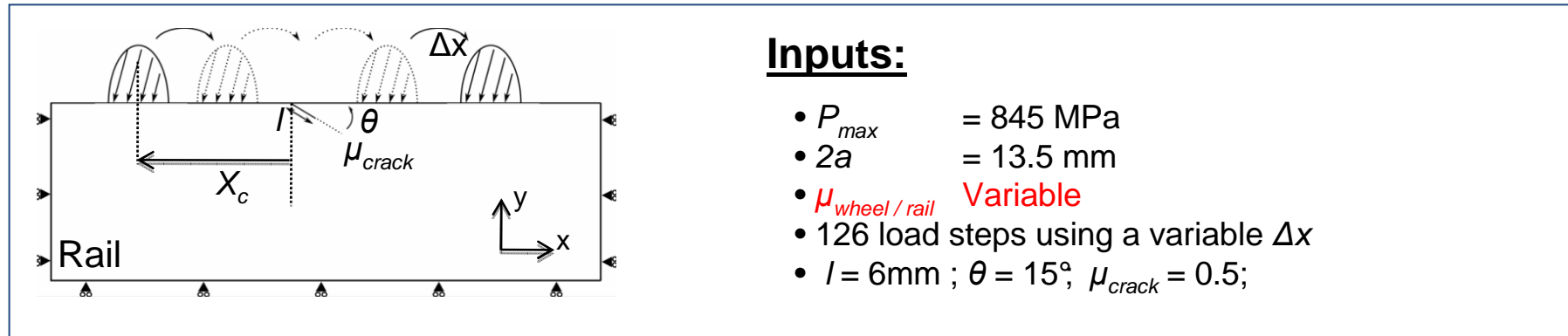
SIF computation for each loading position



Propagation at the end of each cycle



# Influence of the friction coefficient between the wheel and the rail



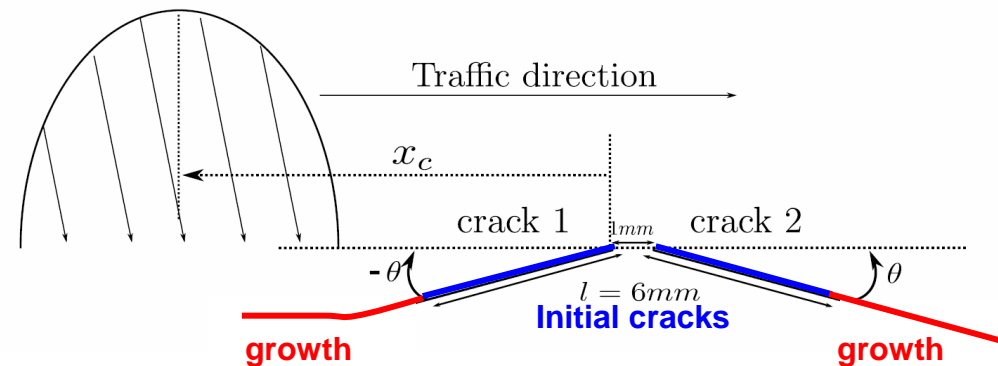
A high tangential loading provokes earlier crack branching upwards or downwards in the rail depending on the direction of the tangential loading.



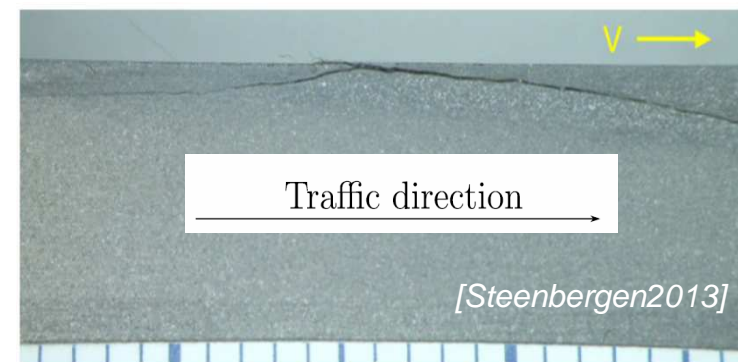
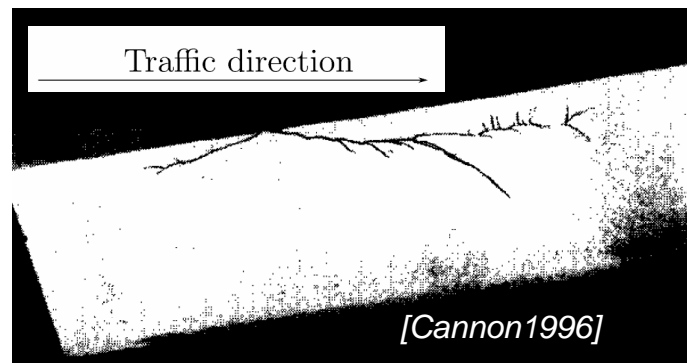
# Crack network : “squat configuration”

## Inputs:

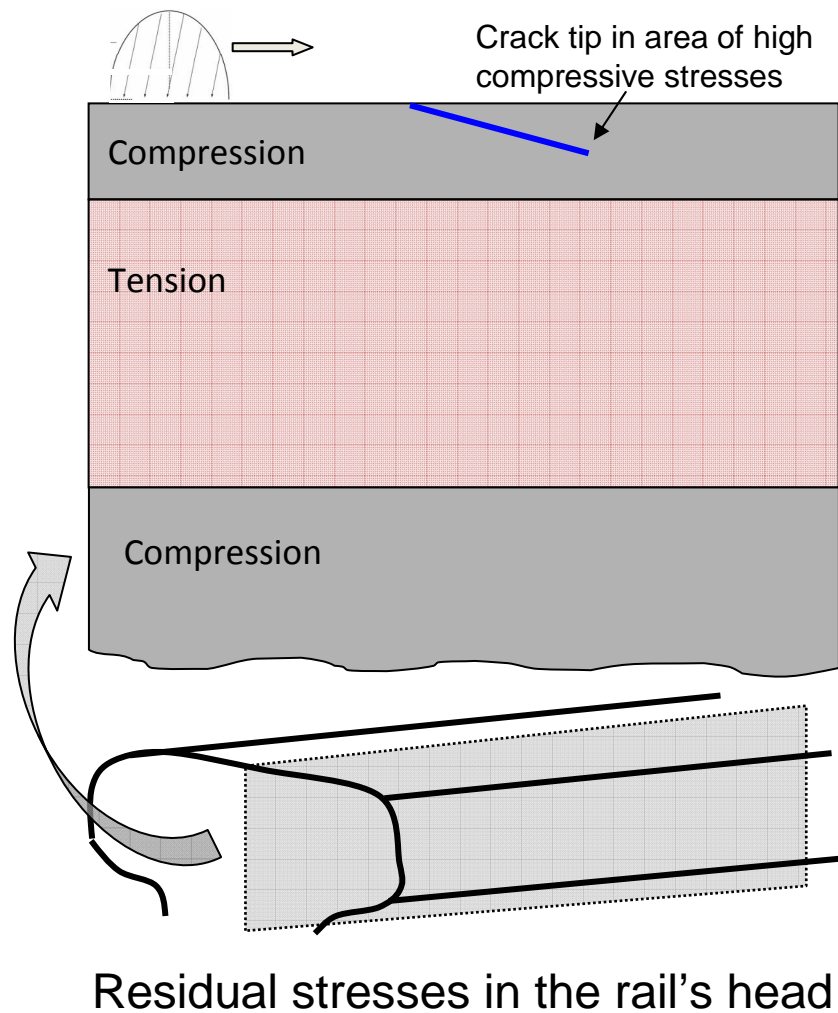
- $P_{\max}$  = 845 MPa
- $2a$  = 13.5 mm
- $\mu_{\text{wheel / rail}}$  = 0.025
- Two initial cracks:
  - $\mu_{\text{cracks}}$  = 0.01
  - $\theta$  =  $15^\circ$



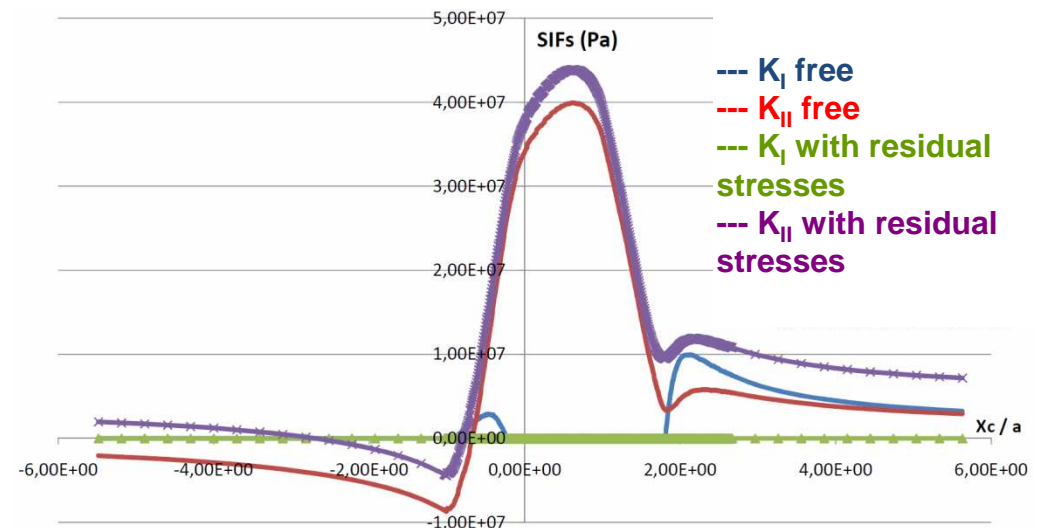
## Longitudinal rail head section through a squat



# Influence of the residual stresses

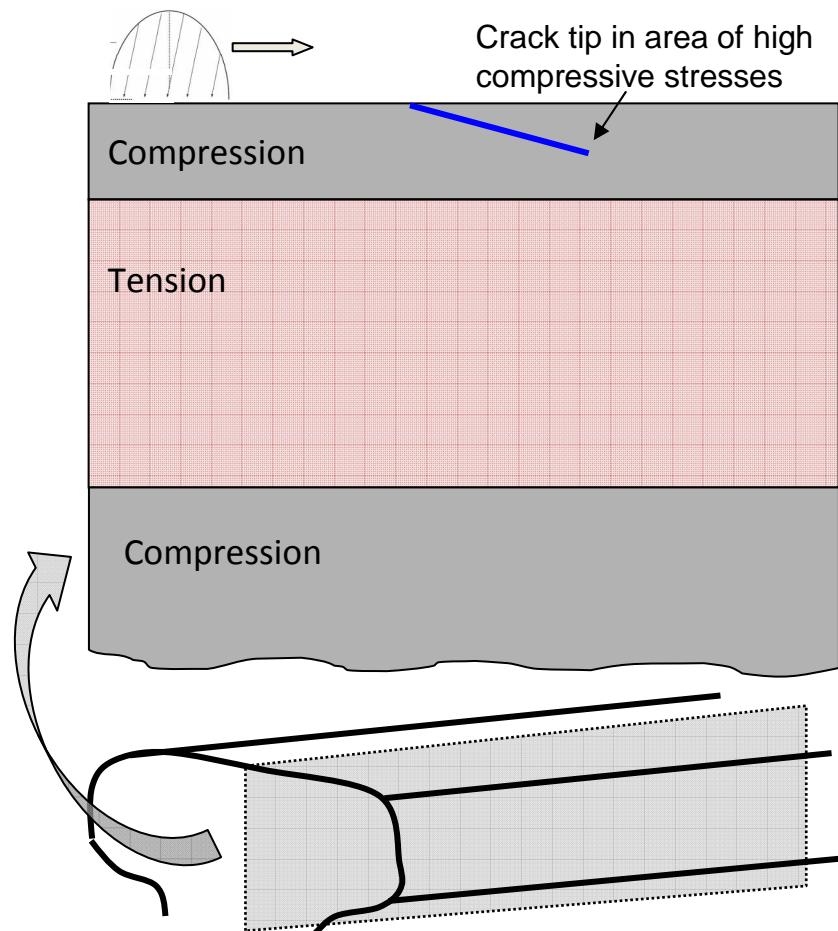


SIF: one loading cycle



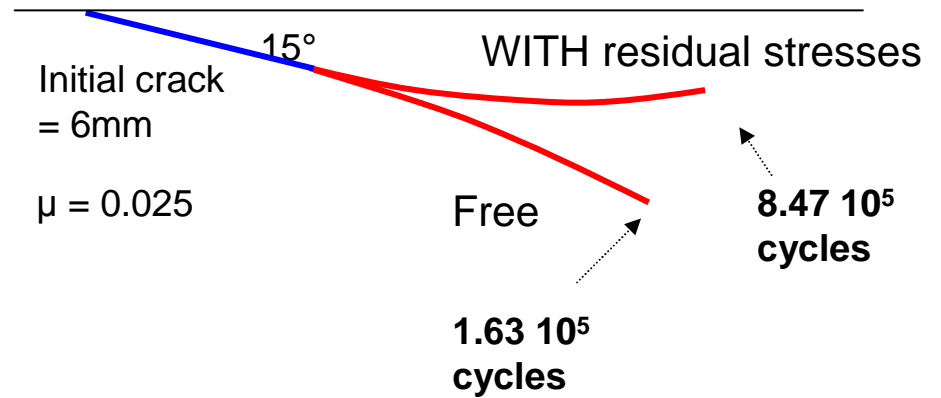
- The crack is always closed during the first loading cycle with residual stresses ( $K_I = 0$ )  
 => Crack growth with shear mode ( $K_{II} \neq 0$ )

# Influence of the residual stresses



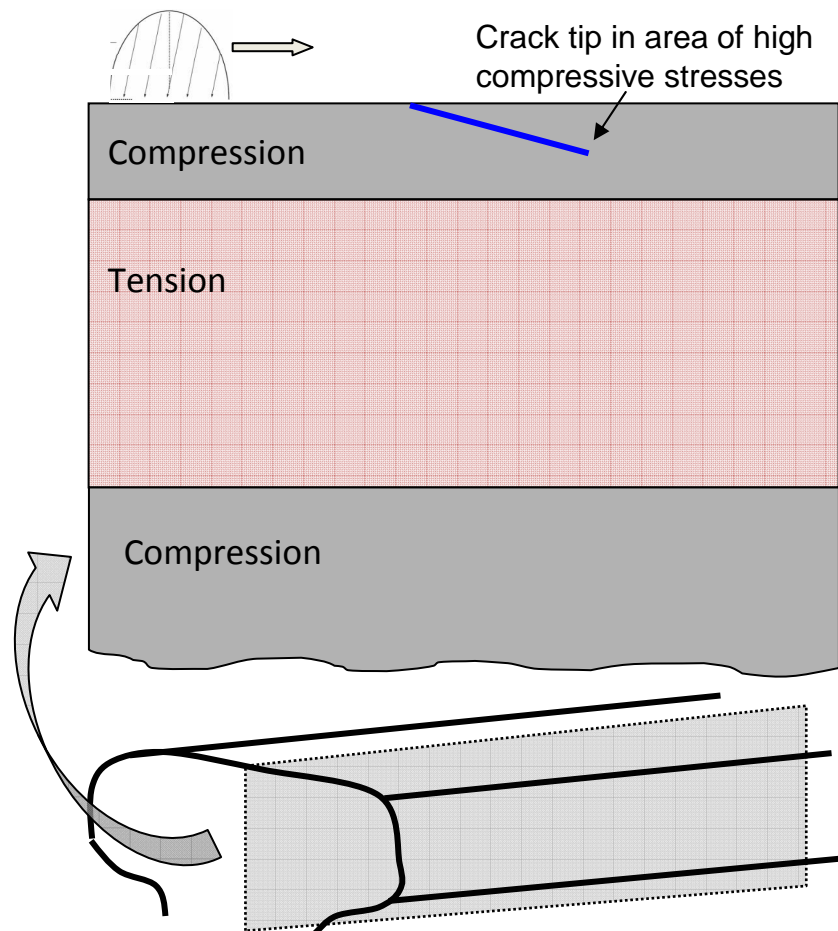
Residual stresses in the rail's head

## Propagation path and crack growth rate

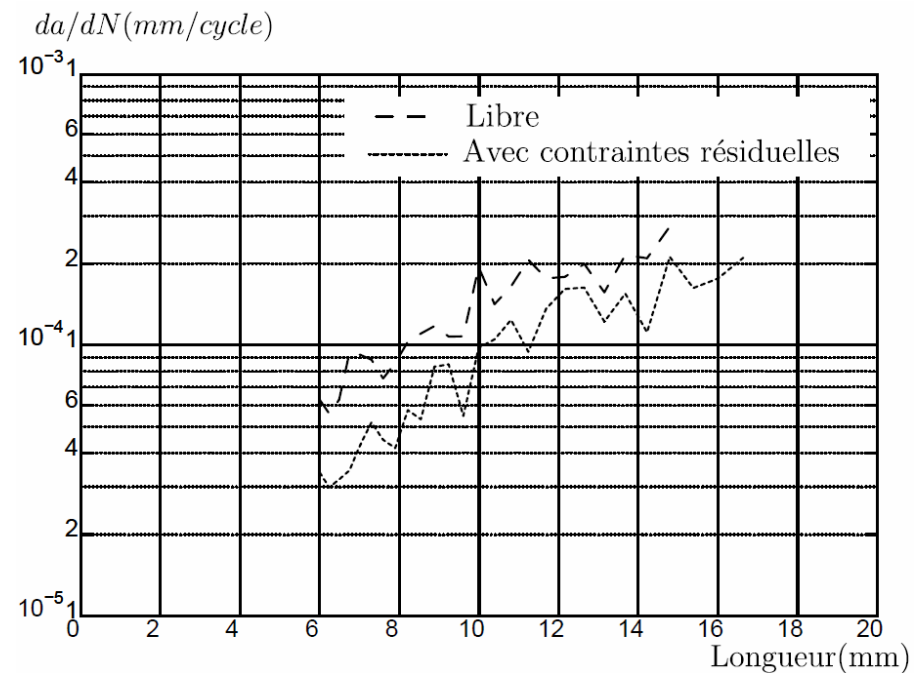


The crack branches upwards with a slower propagation rate if residual stresses are taken into account.

# Influence of the residual stresses

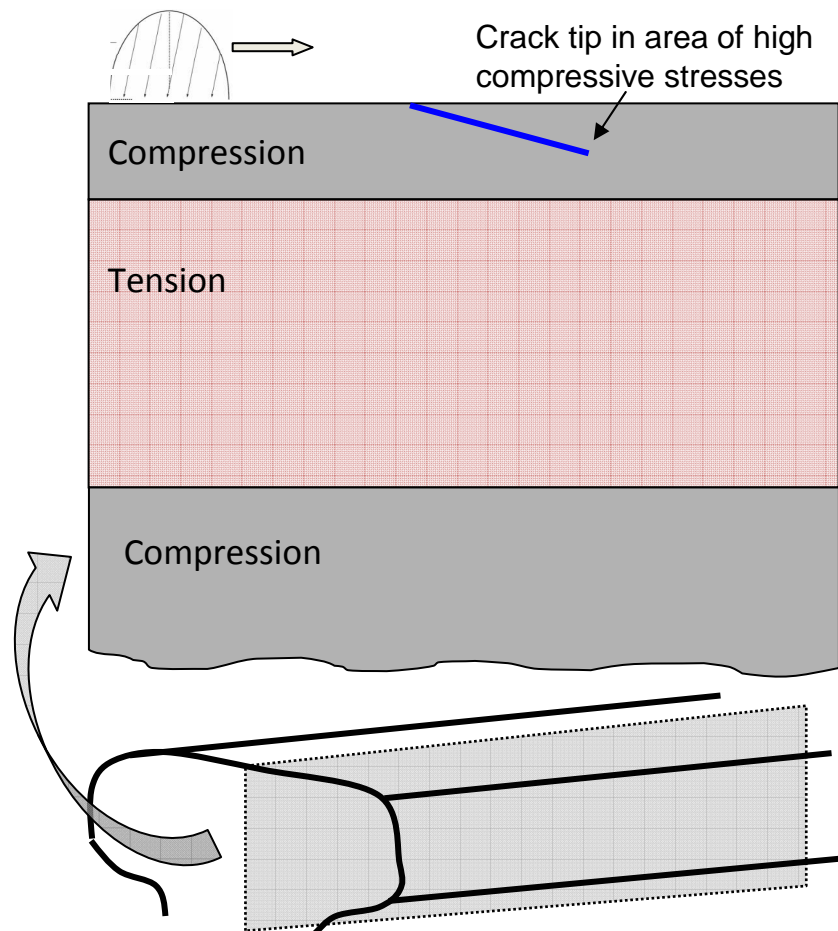


Residual stresses in the rail's head



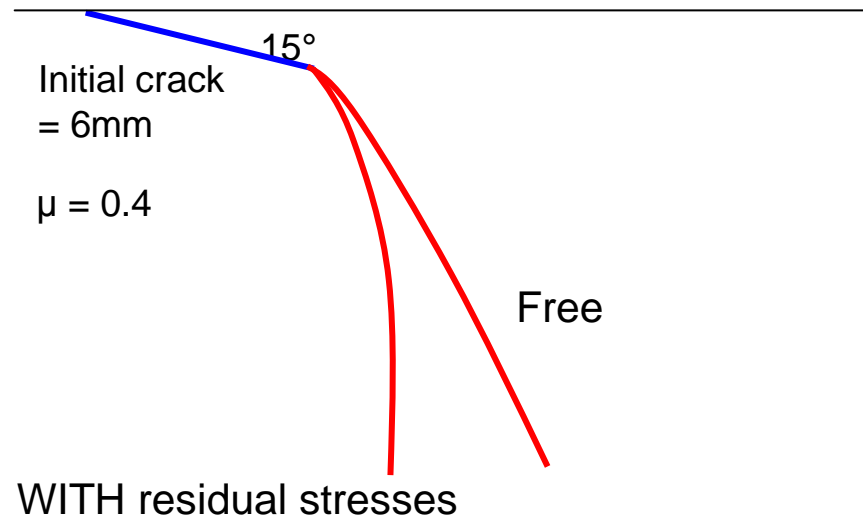
The crack branches upwards with a slower propagation rate if residual stresses are taken into account.

# Influence of the residual stresses



Residual stresses in the rail's head

## Propagation path and crack growth rate



Other inputs

# Outline

- I. Context
- II. Residual stresses in rails
- III. Fatigue crack growth simulations

# IV. Conclusions

# Conclusions

- Two sources of residual stresses in the rail: manufacturing process (C - form) and train passages (local)
- Development of a robust numerical tool to simulate the fatigue crack growth in rails taking into account [Benoit Trollé] :
  - Contact and friction between the crack lips,
  - Mixed mode fatigue law and non-proportional crack branching criterion,
  - Residual stresses (manufacturing process + train traffic),
  - Bending moment (not presented here).
- Rail contact fatigue crack growth simulations: Residual stresses has to be taken into account since they modify the growth rate and the propagation path.

## Acknowledgments

- **LaMCoS**, Laboratory of contact and structural mechanics at INSA Lyon, France (M.-C. Baietto and A. Gravouil)
- **CEA**, French Atomic Energy Commission, in Saclay, France (B.Prabel), [www-cast3m.cea.fr](http://www-cast3m.cea.fr).
- **IDR2** consortium, Initiative for Development and Research on Rails composed by SNCF, RATP, Tata Steel, IFSTTAR, MECAMIX, LAMCOS.

**THANK YOU FOR YOUR ATTENTION !**

[si-hai.mai@sncf.fr](mailto:si-hai.mai@sncf.fr)

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